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Solution studies of vanadium(IV) complexes with nitrilotriacetic acid (NTA) and other aminopolycarboxylic acids (NDAP, NDPA, and NTP)

ML Araujo^a; F. Brito^a; I. Cecarello^a; C. Guilarte^a; JD Martinez^a; G. Monsalve^a; V. Oliveri^a; I. Rodriguez^a; A. Salazar^a

^a Facultad de Ciencias, Centro de Equilibrios en Solución (CES), Escuela de Química, Universidad Central de Venezuela (UCV), Caracas, Venezuela

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Solution studies of vanadium(IV) complexes with nitrilotriacetic acid (NTA) and other aminopolycarboxylic acids (NDAP, NDPA, and NTP)

M.L. ARAUJO*, F. BRITO, I. CECARELLO, C. GUILARTE, J.D. MARTINEZ, G. MONSALVE, V. OLIVERI, I. RODRIGUEZ and A. SALAZAR

Facultad de Ciencias, Centro de Equilibrios en Solución (CES), Escuela de Química, Universidad Central de Venezuela (UCV), Caracas, Venezuela

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Complexes of vanadium(IV) with aminopolycarboxylic acids, nitrilotriacetic (NTA), nitrilodiaceticpropionic (NDAP), nitrilodipropionicacetic (NDPA), and nitrilotripropionic (NTP) acids were studied by electromotrice force measurements [emf(H)] in 3.0 M KCl ionic medium at 25°C. Data analysis using the least-squares program LETAGROP, according to the general reaction $p \text{ H}^+ + q \text{ VO}^{2+} + r \text{ C}^{3-} \leftrightarrows h_p(\text{VO})_q C_r^{p+2q-3r}$, indicates that the following complexes are formed (H₃C ligands): NTA ([VOC]⁻ and [OHVOC]²⁻); NDAP ([VOC]⁻ and [OHVOC]²⁻); NDPA ([VOC]⁻ and [OHVOC]²⁻); and NTP ([H₂VOC]⁺, HVOC, [VOC]⁻, and [OHVOC]²⁻). The following order of coordination capacity NTA > NDAP > NDPA > NTP is suggested, based on values of stability constants and is attributed to the increase in propionic groups in the sequence. The study confirms that five-membered ring chelates are the most stable for V^{IV}, like Cu^{II}, Ni^{II}, lanthanides, and other heavier elements.

Keywords: Solution equilibria; Vanadium(IV) complexes; Aminopolycarboxylic acids; Stability constants; LETAGROP program

1. Introduction

The coordination chemistry of vanadium plays an important role in the interaction with biomolecules [1]. Among the biological functions attributed to vanadium are therapeutic, hormonal, cardiovascular effects and anticarcinogen activity [2–6].

Several studies have been reported on complexes of nitrilotriacetic (NTA), nitrilodiaceticpropionic (NDAP), nitrilodipropionicacetic (NDPA), and nitrilotripropionic (NTP) acids (figure 1) with ions like Cu^{2+} , Ni^{2+} , Co^{2+} , Zn^{2+} , Cd^{2+} , and Mg^{2+} [7].

The present work reports the results of the study of the complexes of vanadium(IV) with these ligands by electromotrice force measurements [emf(H)], in 3.0 M KCl ionic medium at 25°C.

^{*}Corresponding author. Email: maraujo@ciens.ucv.ve

In water solution the oxovanadium(IV) ion, $[VO(H_2O)_5]^{2+}$, briefly VO^{2+} , hydrolyzes at $-\log h > 2.5$ forming $[OHVO]^+$, $[(OH)_2(VO)_2]^{2+}$, and $(OH)_2VO$ [8]. For $-\log h > 4$ $(OH)_2VO$ precipitates, but re-dissolves above $-\log h = 10$ to give clear brown solutions from which brown-black salts such as $K_{12}[V_{18}O_{42}] \cdot 24$ H₂O can be isolated [9].

In connection with vanadium(IV) complexes with the aforementioned ligands, there is only information on complexes with NTA acid, as shown in table 1 [10–14].

In the present investigation the VO²⁺ ion and NTA, NDAP, NDPA and NTP (H₃C) in aqueous solution form *nk* complexes $H_p(VO)_q C_r^{p+2q-3r}$, denoted by (p,q,r), each with a formation constant β_{pqr} , according to the general reaction (1).

$$p\mathbf{H}^{+} + q\mathbf{VO}^{2+} + r\mathbf{C}^{3-} \rightleftharpoons \mathbf{H}_{p}(\mathbf{VO})_{q}\mathbf{C}_{r}^{p+2q-3r}$$
(1)

2. Experimental

2.1. Mass balance equations and symbols

We have for hydrogen ions, vanadium(IV) and ligand concentrations the mass balance equations (2).

$$\begin{aligned} \mathbf{B}Z_{\mathbf{B}} &= \mathbf{C}Z_{\mathbf{C}} = (\mathbf{H} - h + K_{\mathbf{w}}h^{-1}) = \Sigma\Sigma\Sigma p\beta_{pqr}h^{p}b^{q}c^{r} \\ \mathbf{B} &= b + \Sigma\Sigma\Sigma q\beta_{pqr}h^{p}b^{q}c^{r} \\ \mathbf{C} &= c + \Sigma\Sigma\Gamma \beta_{pqr}h^{p}b^{q}c^{r} \end{aligned}$$
(2)

The symbols used are the same as in a previous work, chemicals are in roman and concentrations in italic font [15]. **H**, **B** and **C** represent the total (analytical) concentrations of H⁺, metal and ligand, and *h*, *b* and *c* are the equilibrium concentrations of H⁺, VO²⁺ and C³⁻, respectively; K_w is the water dissociation constant, and the formation functions Z_B and Z_C are defined as the average number of H⁺ bonds per metal and ligand, respectively.

$$\label{eq:ch2} \begin{array}{ccc} ({\rm CH}_2)_{\rm X} & - {\rm COOH} & {\rm NTA}; \, {\rm x}={\rm y}={\rm z}={\rm 1} \\ {\rm N} & \overbrace{\qquad ({\rm CH}_2)_{\rm Y} & - {\rm COOH} \\ & {\rm NDPA}; \, {\rm x}={\rm y}={\rm 1}; \, {\rm z}={\rm 2} \\ {\rm NDPA}; \, {\rm x}={\rm 1}; \, {\rm y}={\rm z}={\rm 2} \\ \end{array}$$

Figure 1. Structural formula of NTA, NDAP, NDPA, and NTP acids.

Table 1. Stability constant values β_{p11} for the vanadium(IV) complexes with NTA acid according to the general reaction (1).

Species	pqr			$\log \beta_{p11}$		
HVOC	111					15.69
[VOC] ⁻	011	10.82	15.34	12.30	11.47	13.18/12.6 (UV–Vis)
[OHVOC] ²⁻	-111	7.23		7.15	7.06	6.07
Ionic medium		0.1 M K NO3	1.0 M (NH4)2SO4	0.5 M NaClO₄	0.1 M KNO3	0.2 M KCl
°C			25			
Method		Emf(H)				
References		[10]	[11]	[12]	[13]	[14]

Using the FONDO concept [16], which consists of subtracting from the total number of associated H⁺, **B**Z_B, or **C**Z_C, and from the total concentrations **C** and **B**, the contribution of the equilibrium concentration of the products of the hydrolysis of VO²⁺ ion, $\Sigma\Sigma pc_{pq0}$, and the equilibrium concentration of the H_pC^{3-p} (p=1-4) ligand acid species, $\Sigma\Sigma pc_{p01}$, and $\Sigma\Sigma c_{p01}$, respectively. We use instead of Z_B and Z_c, the *reduced* formation functions Z_{Bf} and Z_{Cf} (3), where

$$Z_{Bf} = (\mathbf{B}Z_{B} - \Sigma\Sigma pc_{pq0} - \Sigma\Sigma pc_{p01})/(\mathbf{B} - \Sigma\Sigma qc_{pq0})$$

$$Z_{Cf} = (\mathbf{C}Z_{C} - \Sigma\Sigma pc_{pq0} - \Sigma\Sigma pc_{p01})/(\mathbf{C} - \Sigma\Sigma c_{p01})$$
(3)

we only observe the contribution of the species of reaction (1) of interest.

2.2. Emf(H) measurements

The equilibrium emf(H) data [H, B, C, E_0 , J, $(v, E)_{np}]_{ns}$ (E_0 and J = Nernst equation parameters [17], ns = experiments number, np = number of points in each experiment) for the H⁺-VO²⁺ – ligand systems were analyzed by means of the NERNST [18] and FONDO [16] versions of LETAGROP [19]. For this purpose, functions (4)–(8) were minimized with $Z_B^*, Z_C^*, Z_C^*, Z_C^*$,

$$U_1 = \Sigma (Z_{\rm B} - Z_{\rm B}^*)^2 \tag{4}$$

$$U_2 = \Sigma (Z_{\rm C} - Z_{\rm C}^*)^2 \tag{5}$$

$$U_{3} = \Sigma (Z_{\rm Bf} - Z_{\rm Bf}^{*})^{2}$$
(6)

$$U_4 = \Sigma (Z_{\rm Cf} - Z_{\rm Cf}^*)^2 \tag{7}$$

$$U_5 = \Sigma (\mathbf{E} - E^*)^2 \tag{8}$$

and E^* being the respective calculated values according to the probable model of species $(p, q, r, \beta_{pqr})_{nk}$.

Similarly, the equilibrium emf(H) data $[\mathbf{H}, \mathbf{C}, E_0, J, (v, E)_{np}]_{ns}$ for the H⁺ – ligand systems were treated by means of the NERNST version [18], according to reaction (9).

$$pH^+ + C^{3-} \rightleftharpoons H_p C^{3-p} \tag{9}$$

2.3. Materials, solutions, and methods

Used reagents included HCl and KOH, Titrisol, KHCO₃, KCl, NTA, VOSO₄ \cdot 5H₂O Merck, cation exchange Dowex 50 W-X8(H) 50 mesh, O₂ and CO₂ free nitrogen, and triply-distilled water. The analytical methods are the same as detailed in reference [8a] and the emf(H) titration method described in [20] was used.

The ligands NDAP, NDPA, and NTP were synthesized [21], 3.0 M (H⁺, K⁺)Cl (={ H^+ }), H_o mM in H⁺, and 3.0 M K(OH⁻, Cl⁻) (={ OH^- }), A_o mM in OH⁻ solutions were prepared by weighing dry KCl, adding HCl and KOH (0.100 M ampoules), in the presence of nitrogen, and standardized the first one *versus* Na₂CO₃ [22] and the second *versus* this last one, using the Gran method [23], respectively.

Vanadium(IV) 3.0 M ($\frac{1}{2}$ VO²⁺, H⁺, K⁺) Cl (={VO²⁺}) solution was prepared by extracting the VO²⁺ ion with 3.0 M KCl from a cationic exchange resin saturated with VO²⁺ and H⁺ ions, followed by dilution, gauging, and finally titration in H⁺ and vanadium(IV) [24].

Potentiometric titrations were carried out in a Metrohm BT 8-02 reaction cell of about 100 mL, with double walls and several mouths for inserting tubes for gas charge and discharge, measuring electrodes and a burette for the addition of reagents. The measurements were performed with bubbling nitrogen and under magnetic agitation.

The concentration of H⁺ in equilibrium *h* was determined by means of the cell REF// *S/EV*, where *EV* denotes the glass electrode, *S* is the equilibrium solution, and REF (=KCl 3.0 M/KCl 3.0 M, Hg₂Cl₂/Hg, Pt), the reference half-cell. The potential (mV) of the cell at 25°C is given by the Nernst equation $E = E_0 + Jh + 59.16 \log h$, with E_0 as its normal potential and *J* a constant related to the potential at the liquid junction [17].

The experiments were carried out in two successive stages. The first stage consists of a strong acid-base titration to determine the parameters E_0 and J of the Nernst equation and the second stage is the experiment.

After determination of acidity constants of the ligands in the first stage, the second consisted of adding a weighed quantity of H₃C, and later titrating with { \mathbf{H}^+ } and/or { \mathbf{OH}^- } solutions. For determination of the stability constants of the complexes, the second stage consisted of adding an aliquot of the { \mathbf{VO}^{2+} } solution, a weighed quantity of ligand H₃C using the ligand: metal ratios R = 1 and 2, and then titrated with { \mathbf{H}^+ } and/or { \mathbf{OH}^- } solutions.

3. Results and discussion

3.1. Ionization constants of the acids

The p K_i values presented in table 2 were calculated from the values of β_{p01} defined in the equilibrium reactions (9).

The validity of the values found is proven by the good fit between the experimental $Z_c(\log h)$ curve (dotted curve) and the $Z_c^*(\log h)$ calculated curve (continuous line), as can be observed in figure 2 for NTA, NDPA, NDAP, and NTP acids.

The values of pK_i for all the acids are in good agreement with literature data [25]. These ligands show an acidity order NTA>NDAP>NDPA>NTP due to the successive substitution of acetic groups by propionic groups, which have a greater

Table 2. pK_i values of NTA, NDAP, NDPA, and NTP acids (H₃C) in 3.0 M KCl ionic medium at 25°C.

	$pK_i(3\sigma)$			
Equilibrium	NTA	NDAP	NDPA	NTP
H ₄ C ^{+/} H ₃ C	1.33(3)	1.12(4)	1.81(6)	3.14(9)
H_3C/H_2C^-	1.76(1)	2.30(2)	3.42(3)	3.97(5)
H_2C^{-}/HC^{2-}	2.48(2)	3.83(4)	4.28(5)	4.39(7)
HC^{2-}/C^{3-}	9.45(3)	9.47(5)	9.76(7)	9.72(7)
$\sigma(Z_{\rm c})$	0.011	0.018	0.033	0.015

inductive electronic donor effect because of the presence of another CH₂ group [7]. The values of $pK_{H4C/H3C}$, $pK_{H3C/H2C}$, and $pK_{H2C/HC}$ correspond fundamentally to carboxyl protons, and the values of $pK_{HC/C}$ for all ligands are in agreement with the protonation of the *N* atom in aqueous solution. The diagrams of the distribution of species show that mono-protonated HC^{2-} is the most stable and abundant species, and species containing protonated carboxylic groups improve their stability as the number of propionic groups increases [21]. The diagram corresponding to NTA is presented in figure 3. The H₄C⁺, H₃C and H₂C⁻ species prevail to $-\log h \leq 3$. This last one becomes dominant in the interval $4 \leq -\log h \leq 9$, which in turn loses the last H⁺ to form the basic species C³⁻, that prevails for $-\log h \geq 10$.

3.2. Stability constants of the complexes formed

Analysis of the experimental data of V(IV) – ligand systems allowed us to calculate the β_{pqr} constants for the complex formed for each ligand, defined by means of equilibrium reaction (1).

Taking into account the species resulting from the ionization of the ligand (*vide supra*) as well as the hydrolytic species of vanadium(IV) existing, i.e., $[OHVO]^+$, $[(OH)_2(VO)_2]^{2+}$, and $(OH)_2VO$, whose formation constants at this temperature and



Figure 2. Z_c , average number of H⁺ associated per mol of ligand versus $-\log h$ for NTA(+), NDAP(Δ), NDPA(\Box) and NTP(\times) acids (H₃C) in 3.0 M KCl ionic medium at 25°C. The lines represent theoretical curves calculated with the pK_i values of table 1.



Figure 3. $Z_c(-\log h)$ data and species distribution diagram for NTA acid (H₃C) in 3.0 M KCl ionic medium at 25°C, for C = 10 mM.

Species			$\log \beta_{pqr}(3\sigma)$	·)	
HVOC [VOC] ⁻ [OHVOC] ²⁻ [(OH) ₂ VOC] ³⁻ $\sigma(Z_{\rm B})$	12.8(3) 12.74(2) 5.59(2) -5.4(1) 0.18	12.9(2) 12.74(1) 5.60(1) -5.40(7)	$13.0(2) \\ 12.76(1) \\ 5.61(2) \\ -5.4(1)$	$13.1(2) \\ 12.76(1) \\ 5.62(2) \\ -5.4(1)$	13.9(<14.2) 12.77(2) 5.62(2) -5.3(1)
$\sigma(Z_{\rm C}) \sigma(Z_{\rm Bf}) \sigma(Z_{\rm Cf}) \sigma(E)(\rm mV)$		0.009	0.017	0.016	2.3

Table 3. Equilibrium constants β_{pqr} for the system H⁺ – VO²⁺ – NTA (H₃C) in 3.0 M KCl ionic medium at 25°C, according to reaction (1).



Figure 4. (a) $Z_{\rm C}$ versus $-\log h$ for the system H⁺ $- \rm VO^{2+} - \rm NTA$ (H₃C) in 3.0 M KCl ionic medium at 25°C, for **B** = 3.0 mM and ratios $R = 1.37(\Box)$, 2.25(+) and 2.30(Δ), according to reaction (1). The lines represent theoretical curves calculated with the equilibrium constants of table 3 (column 3). (b) Species distribution diagram $C_{\rm pqr}(-\log h)$ for **B** = 3.0 mM and ratio R = 2.0 (right ordinate).

ionic medium were determined in previous work [8], the results of this analysis for the H^+ – VO^{2+} – NTA system are given in table 3, with equilibrium constants and standard deviations $\sigma(Z_B)$, $\sigma(Z_C)$, $\sigma(Z_{Bf})$, $\sigma(Z_{Cf})$, and $\sigma(E)$ determined with NERNST [18] and FONDO [16], versions of LETAGROP [19]. The values obtained are of the same order of magnitude.

The validity of these results are displayed in figure 4, where an excellent fit can be observed between the experimental $Z_{\rm C}$ versus $-\log h$ curves and those calculated. This figure also shows the species distribution diagram for $\mathbf{B} = 3.0 \text{ mM}$ and ratio R = 2.0. The most abundant complexes are [VOC]⁻ and [OHVOC]²⁻, but for $-\log h < 2$ and $-\log h > 9$ small quantities of HVOC and [(OH)₂VOC]³⁻, respectively, are formed.

Finally, table 4 contains a summary of the equilibrium constants for the other three systems studied, i.e., $H^+-VO^{2+} - NDAP$, $H^+-VO^{2+} - NDPA$, and $H^+-VO^{2+} - NTP$. In none is $[(OH)_2VOC]^{3-}$ formed, although $[H_2VOC]^+$ is observed in small quantities for the $H^+-VO^{2+} - NDPA$ and $H^+-VO^{2+} - NTP$ systems. Analogous curves to figure 4 are obtained for these three systems.

Usually an increase of chelate ring size leads to a decrease in complex stability [26]. In our case, the order of stability of the vanadium(IV) complexes with the aminopolycarboxylic acids studied is NTA>NDAP>NDPA>NTP. With NTA vanadium(IV) can form five-membered ring chelates, while NTP could form only six-

		$\log \beta_{pqr}(3\sigma)$	
Species	NDAP	NDPA	NTP
$[H_2VOC]^+$ $HVOC$ $[VOC]^-$ $[OHVOC]^{2-}$	14.1(1) 12.60(7) 5.4(1)	15.9(4) 13.5(2) 11.19(1) 4.01(3)	16.7(1) 12.7(1) 8.60(5) 3.17(9)

Table 4. Equilibrium constants β_{pqr} H⁺ – VO²⁺ – H₃C (H₃C = NDAP, NDPA, and NTP) in 3.0 M KCl ionic medium at 25°C, according to reaction (1).

membered ring chelates. That is, as the acetic groups are replaced by propionic groups they diminish the stability of the complexes with six-membered ring chelates.

Therefore, it has been confirmed that five-membered ring chelates are most stable for V(IV), like Cu(II), Ni(II), lanthanides and other heavier elements, while Be(II) and other elements of the first short period prefer six-membered ring chelates [21].

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